

Optimum Step for multistep prediction blind equalizer

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Abstract

Blind equalizers may be implemented with linear prediction error filters (LPEF) but the delay (D) cannot be controlled with one-step predictors to minimize the mean square error (MSE). Consequently, multi-step prediction error filters (MSPEF) has been suggested as a solution to the problem. In this paper, a blind equalizer composed of the Godard algorithm (CMA) cascaded with MSPEF is proposed (CMA_MSPEF), and we extract the optimum value of step for multi-step prediction blind equalizer. Simulation results show comparable improvements of the proposed equalizer relative to the LPEF or the MSPEF equalizers with optimum step.

Keywords: blind equalizers, CMA equalizers and Multistep equalizers.

1. Introduction

A communication channel may introduce inter-symbol interference (ISI) in the received sequence. Blind equalization attempts to remove the ISI without a training sequence. If multiple samples per symbol are available at the receiver, blind equalizers can be derived from the second order statistics (SOS) of the received signal [4][6][8][9]. MMSE equalizers can be implemented with linear multi-channel prediction-error filters [1, 2]. For many practical channels, a small equalization error may be achieved by controlling the delay. Multi-step prediction has been suggested as a solution to the arbitrary-delay equalization problem [2][7]. The organization of the paper is as follows: the system model and the proposed algorithm are presented in Section 2. Simulation results are summarized in Section 3. Concluding remarks in Section 4, are summarized.

2. The CMA – MSPEF Proposed Model Algorithm

The proposed algorithm consists of a linear equalizer constant modulus algorithm (CMA) and multi-step forward prediction error filter (MSPEF) in cascade. The continuous time received signal is:-

$$a(t) = \sum_{k=-\infty}^{\infty} s(k) h(t-k) + v(t) \quad (1)$$

where $s(k)$ is the sequence of complex information symbols, $h(t)$ is the complex baseband channel impulse response, and $v(t)$ is an additive white Gaussian noise (AWGN). The fractionally spaced discrete-time model can be obtained by oversampling. A single-input single-output (SISO) system model results when the sampling rate at the receiver equals the symbol transmission rate. When several samples per symbol interval are taken, the system becomes single-input multiple-output (SIMO) as in fig.1

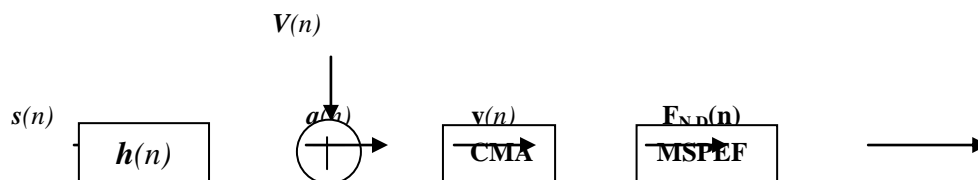


fig .1. The CMA – MSPEF Proposed System

The corresponding SIMO model consists of P sub- channels ($P \geq 2$). The i th subchannel response is defined as $h_i(n) = h(t_o + i/P + n)$ where $n=0,1,2,\dots, L-1$, and L is the subchannel length. Its output $a_i(n) = a(t_o + i/P + n)$ is given by :

$$a_i(n) = \sum_{k=0}^{L-1} s(k) h_i(n-k) + v_i(n) \quad (2)$$

where $0 \leq i \leq P-1$, and $v_i(n)$ are samples of $v_i(t)$ corresponding to $a_i(n)$. In each symbol interval, $\mathbf{a}(n)$ of length P is received in vector form as :

$$\mathbf{a}(n) = [a_0(n), a_1(n), a_2(n), \dots, a_{p-1}(n)]^T \quad (3)$$

The channel impulse response can also be represented in vector form as :

$$\mathbf{h}(n) = [h_0(n), h_1(n), h_2(n), \dots, h_{p-1}(n)]^T \quad (4)$$

and the noise as :

$$\mathbf{v}(n) = [v_0(n), v_1(n), v_2(n), \dots, v_{p-1}(n)]^T \quad (5)$$

where $[\]^T$ denoting transposition .

For the system under consideration, we have assumed the following:

- The input sequence $s(t)$ is zero-mean with unit variance.
- The additive white Gaussian noise $v(t)$ is zero-mean with variance σ^2 .
- The sequences $s(t)$ and $v(t)$ are uncorrelated .

2. a. Adaptation for the CMA equalizer

The adaptation algorithm for the weight of CMA equalizers is as follows [7] :

$$w_i(n+1) = w_i(n) + \mu_f (C - |y_i(n)|^2) y_i(n) A_i^*(n), \quad 0 \leq i \leq P-1 \quad (6)$$

where $y_i(n)$ and the $w_i(n)$ are the outputs and weights of the i^{th} equalizer of length (M_1+M_2+1) . The outputs and weights in vectors the following is obtained:

$$\mathbf{y}(n) = [y_0(n), y_1(n), y_2(n), \dots, y_{p-1}(n)]^T \quad (7)$$

$$\mathbf{w}(n) = [w_0(n), w_1(n), w_2(n), \dots, w_{p-1}(n)]^T \quad (8)$$

Finally, C is the modulus given by [7] :

$$C = E\{|s(n)|^4\} / E\{|s(n)|^2\} \quad (9)$$

and μ_f is the step size given by :

$$\mu_f = .001 / E[|s(n)|^4] \quad (10)$$

$A_i^*(n)$ is the corresponding input vectors with length equal to (M_1+M_2+1) .

2.b. Adaptation for the MSPEF equalizer

Stacking previously N output vectors of the CMA equalizers each of length into an $(NP \times I)$ vector, then the MSPEF input can be represented as:

$$\mathbf{y}_N(n) = [\mathbf{y}^T(n), \mathbf{y}^T(n-1), \mathbf{y}^T(n-2), \dots, \mathbf{y}^T(n-N+1)]^T \quad (11)$$

A D -step forward predictor of order N produces an estimate $\hat{s}(n)$ of the received symbol $s(n)$ based on the N previous symbols $y_N(n-D)$. The MSPEF coefficients $U_{N,D}$ are obtained from Yule Walker Equations [3] as :

$$U_{N,D} = E\{y_{N-D+1}(n-D) \mathbf{y}^+(n)\} (R_{N-D+1}^{-1}) \quad (12)$$

where R_{N-D+1} is the covariance of $\mathbf{y}_{N-D+1}(n)$,

$(\)^+$ and $E(\)$ denoting transpose conjugation and statistical expectation respectively . A corresponding D -step forward prediction

error filter (PEF) of order N produces the error $f_{N,D}(n) = s(n) - \hat{s}(n)$ as its output. The D -step prediction error is then:

$$f_{N,D}(n) = U_{N,D} y_{N+D}(n) \quad (13)$$

The blind equalization method considered here is based on the output of D and $(D+1)$ -step prediction error filter's [7], so the output of **CMA_MSPEF** is given by:

$$F_{N,D}(n) = f_{N,D+1}(n) - f_{N,D}(n) \quad (14)$$

where $f_{N,D+1}(n)$ is the output of $D+1$ -step predictor and $f_{N,D}(n)$ is the output of D -step predictor.

3. Simulation Results

The proposed system was applied to 16-QAM and 4-QAM modulation techniques with additive white Gaussian noise. The performance of the **CMA_MSPEF** system is obtained via simulation to extract the optimum step D , for the following three channels given below and which were considered in [1], [3] and [7].

Channel one: $(0.1632+j0.2056), (-0.9491+j0.1524), (1+j0),$

$(0.2393-j0.0077), (0.0041-j0.5634),$

$(0.0041-j0.5634), (-0.2452+j0.7152),$

$(0.8+j0), (-0.2393+j0.1775).$

Channel two: $(-0.05+j0.27), (-0.37-j0.01), (0.02-j0.07),$

$(-0.21-j0.03), (0.5-j0.6), (0.25+j0.27),$

$(-0.1+j0.38), (0.22-j0.05), (0.26+j0.14),$

$(0.17-j0.72).$

Channel three: $(-0.005-j0.0004), (0.009+j0.0300),$

$(-0.024-j0.1040), (0.854+j0.5200),$

$(-0.218+j0.2730), (0.049-j0.0740),$

$(-0.016+j0.0200), (0.010+j0.0002),$

$(-0.018-j0.0150), (0.048+j0.0520),$

$(1+j0), (0.436+j0.1360), (-0.098+j0.0370),$

$(0.032-j0.0100).$

The parameters used in the simulation are: $M_1=M_2=N=15$. Depicted results shown in figures (2-10), give the MMSE versus iterations for different channels, different SNR and the employed modulation techniques.

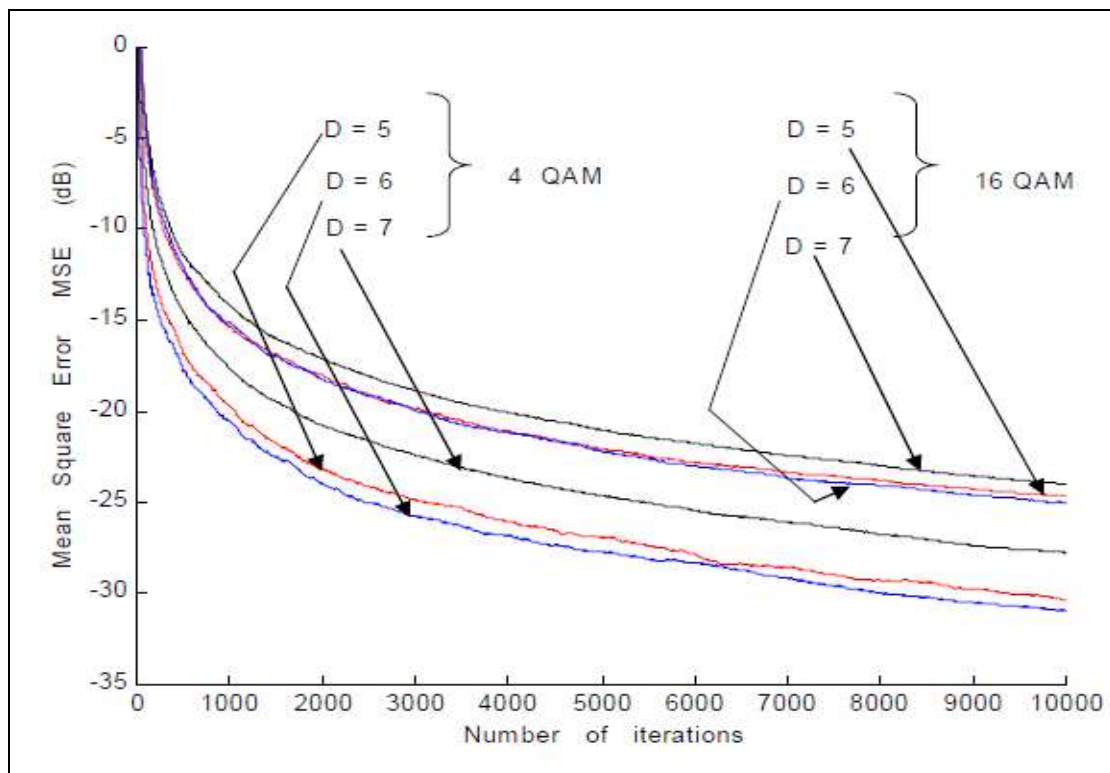


Fig.2. Optimum Step D for Channel one and SNR=0 dB

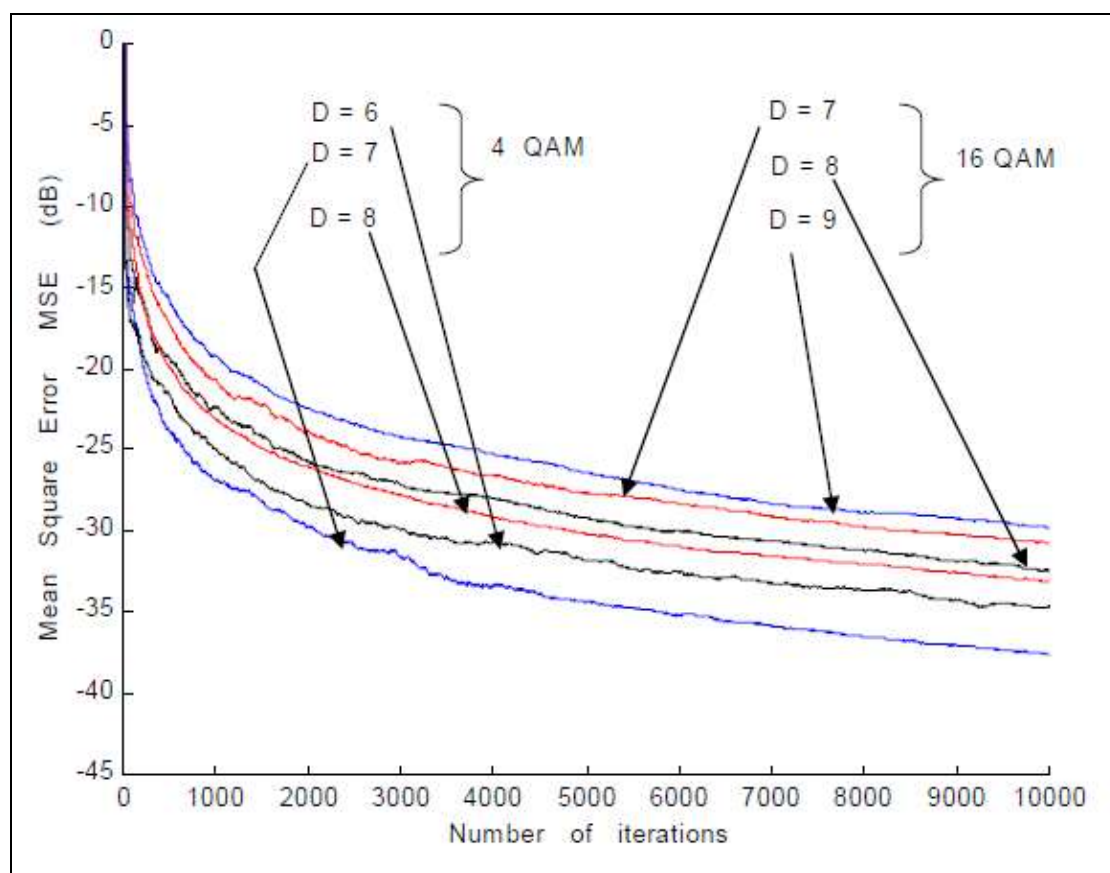


Fig.3. Optimum Step D for Channel one and SNR=5 dB

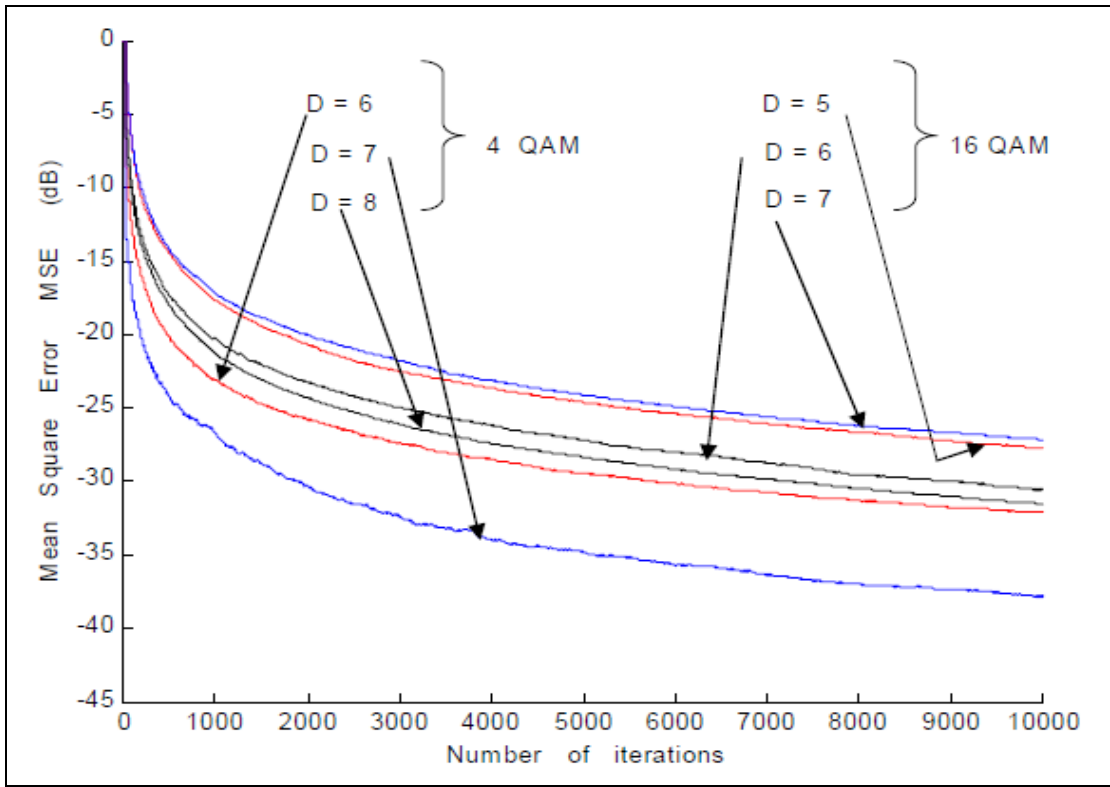


Fig.4. Optimum Step D for Channel one and SNR=10 dB

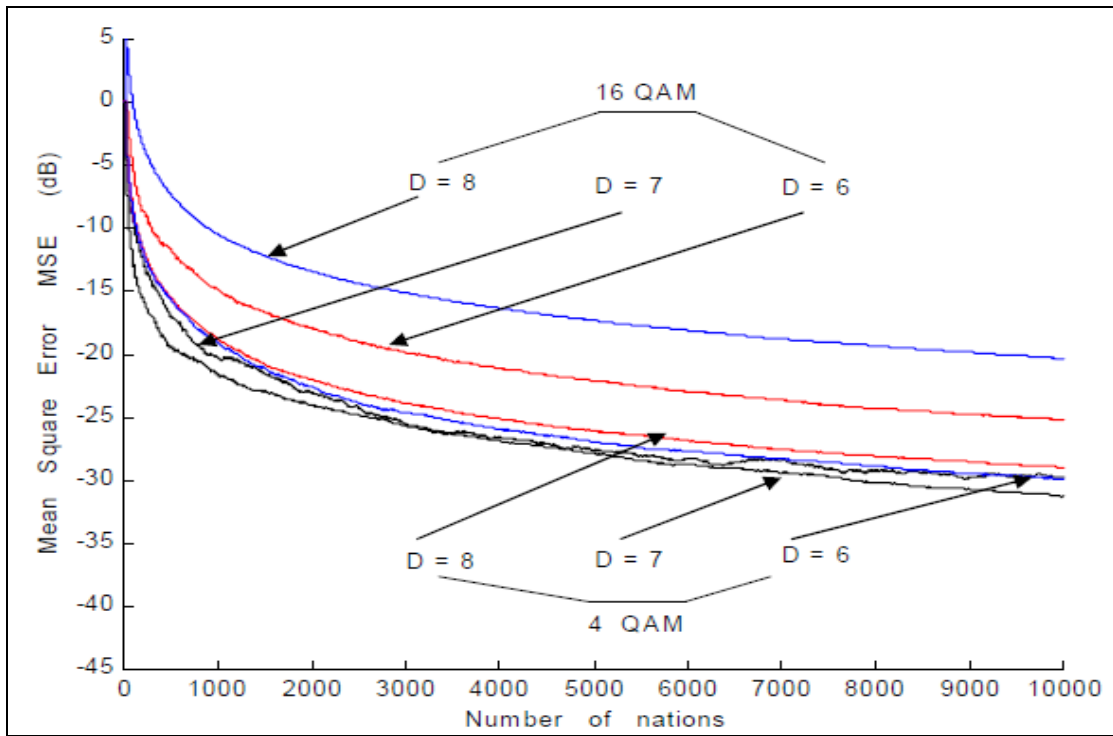


Fig.5. Optimum Step D for Channel Two and SNR=0 dB

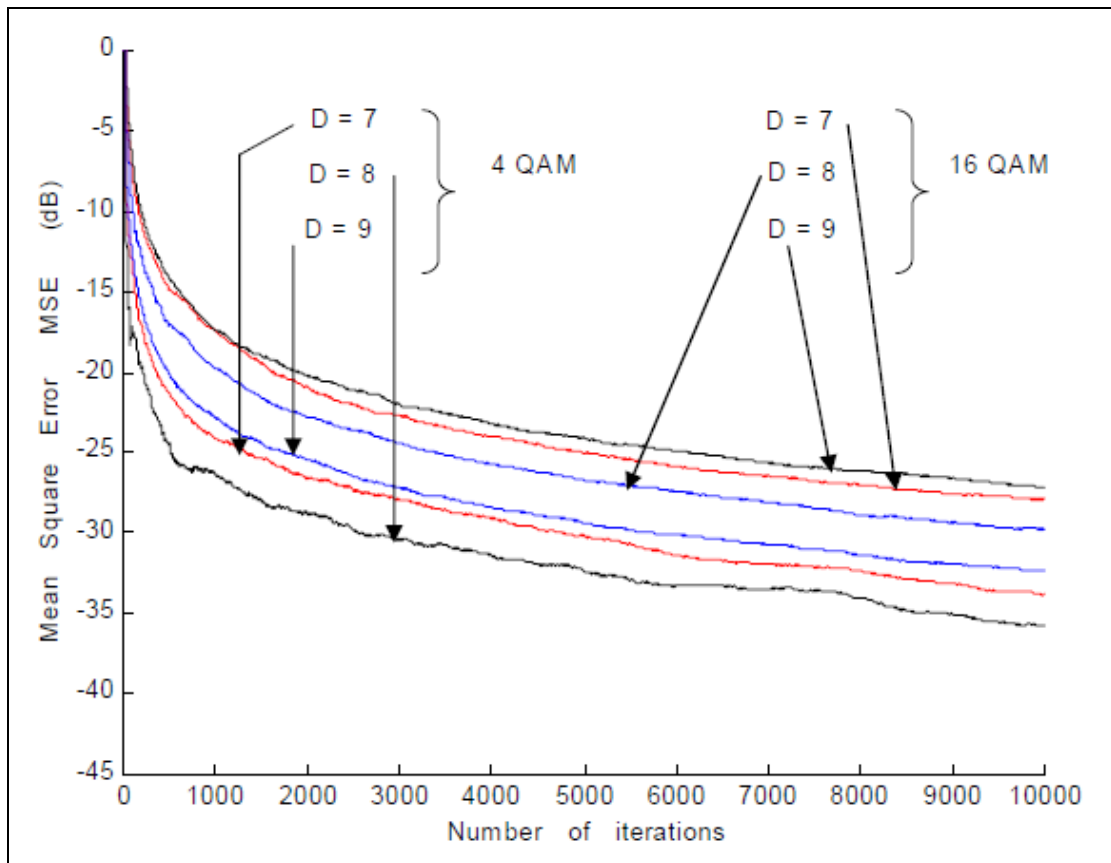


Fig.6. Optimum Step D for Channel Two and SNR=5 dB

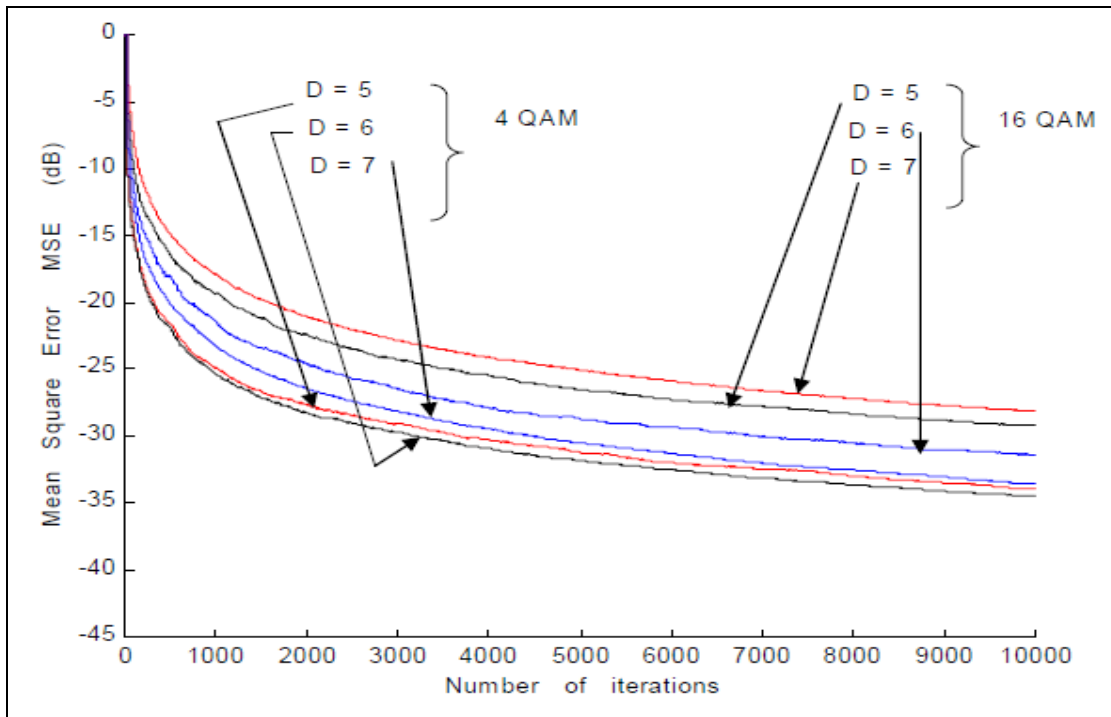


Fig.7. Optimum Step D for Channel Two and SNR=10 dB

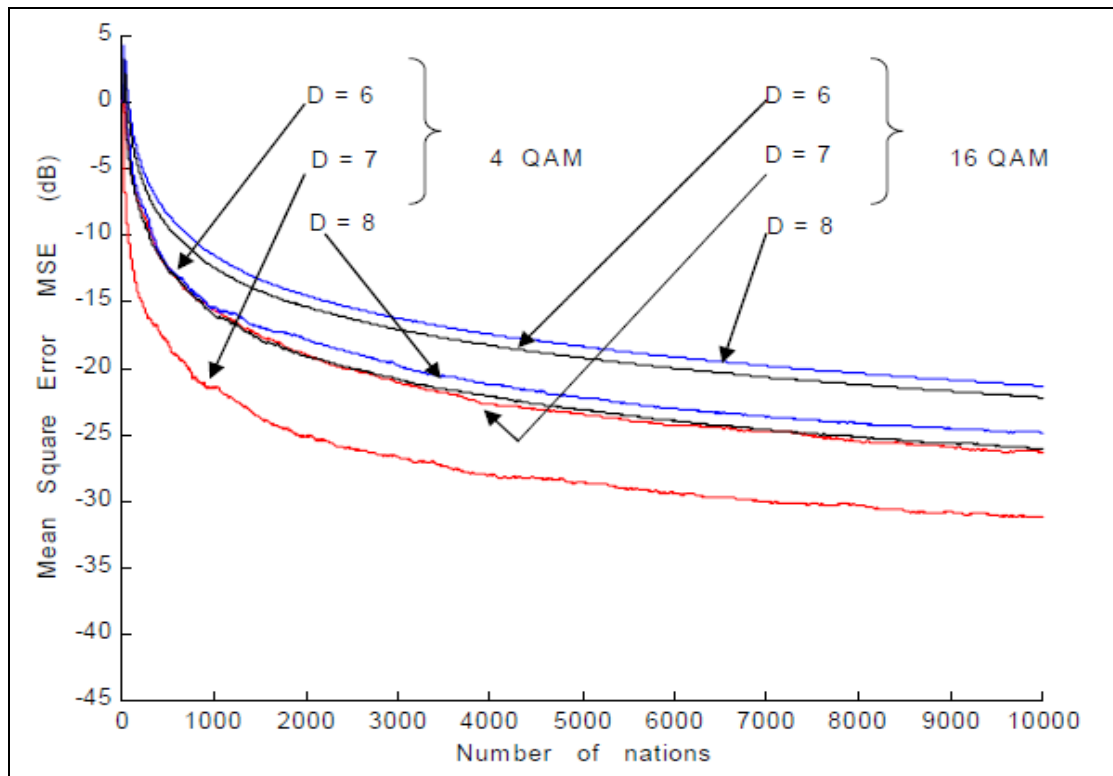


Fig.8. Optimum Step D for Channel Three and SNR=0 dB

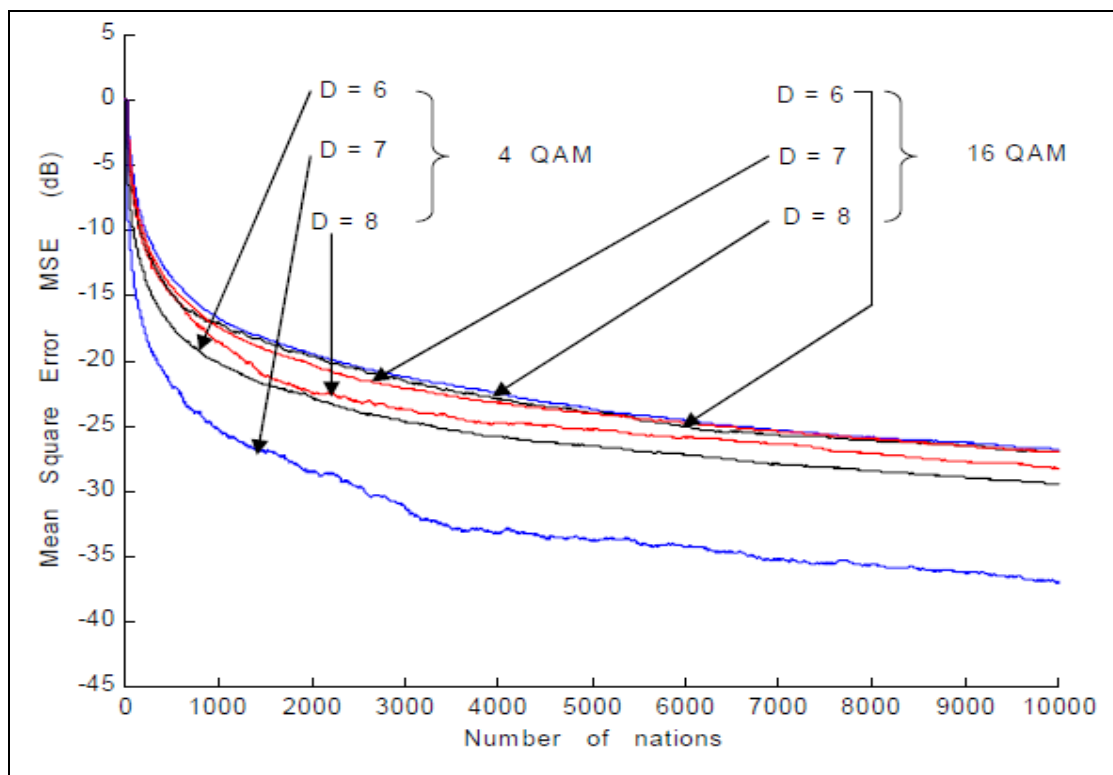


Fig.9. Optimum Step D for Channel Three and SNR=5 dB

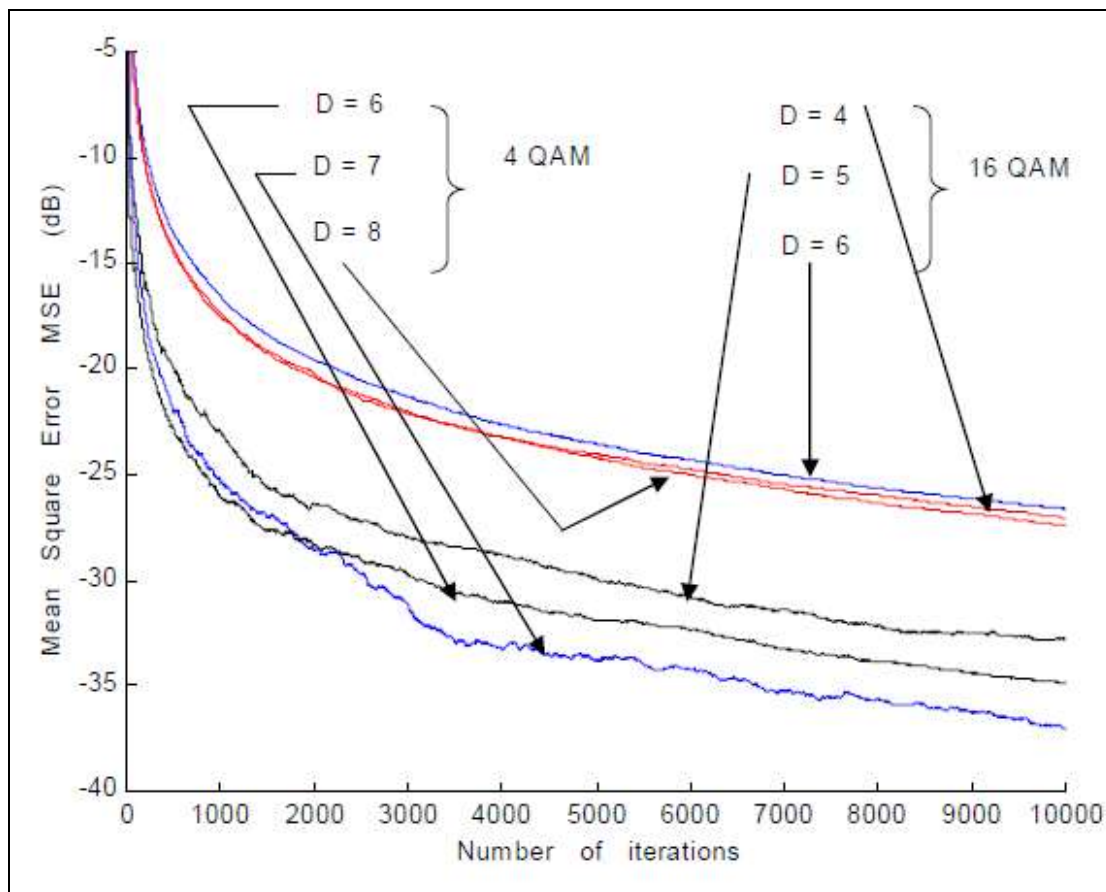


Fig.10. Optimum Step D for Channel Three and SNR=10 dB

Figures (2-10), show the optimum value of D for the three channels as follow:

(a) For SNR = 0 dB,

The optimum value of D is equal (7) for 4 QAM and 16 QAM.

(b) For SNR = 5 dB,

The optimum value of D is (8) for 4 QAM and it is equal (7) for 16 QAM

(c) For SNR = 10 dB,

The optimum value of D is (6) for 4 QAM and it is equal (7) for 16 QAM

From the previous values, it is clear that D is dependent on the SNR and the modulation technique even for the same channel. So optimum **D=7** for **channel one**, optimum **D=8** for **channel two**, and optimum **D=6** for **channel three**. Furthermore, it varies from a channel to the other.

The MSE simulation comparative results for channel two versus the number of iterations (10000) for the CMA , LPEF, MSPEF and CMA_MSPEF are depicted in fig.11 .

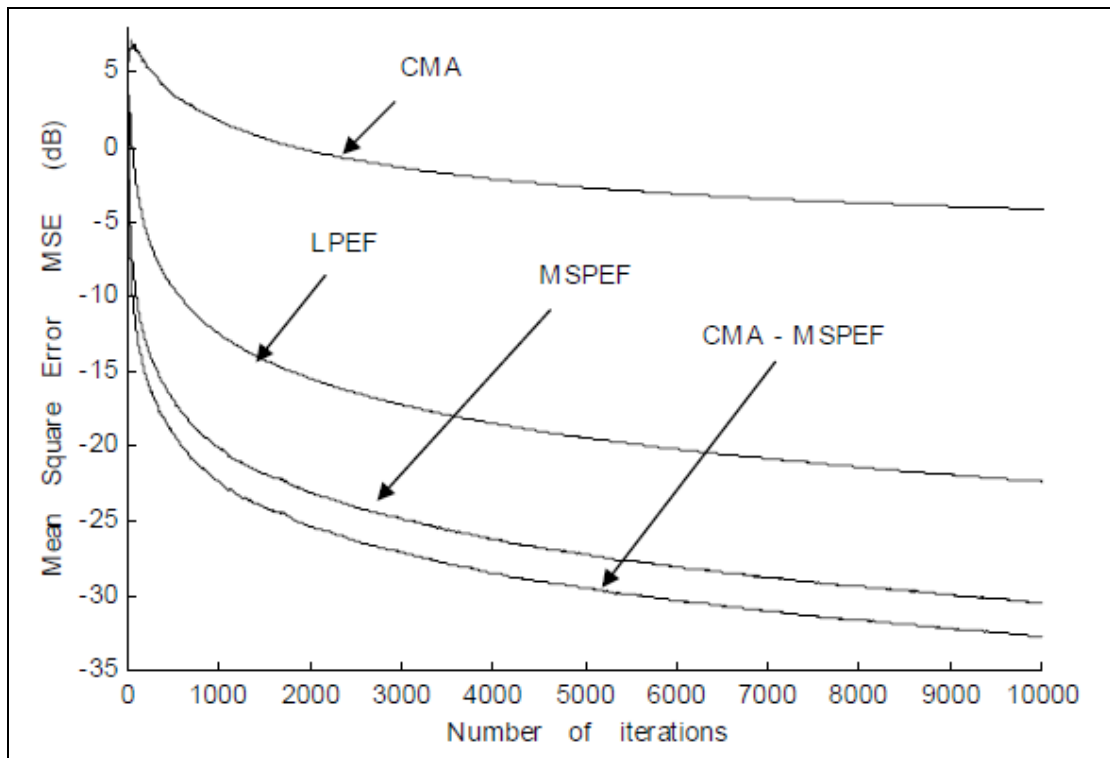


Fig.11. Comparison between CMA, LPEF, MSPEF, and CMA_MSPEF

Figure (11) shows that the proposed algorithm CMA_MSPEF dominates the three algorithms CMA, LPEF, and MSPEF, for channel two, $D = 8$, 16 QAM, and $SNR=10$ dB. From this figure, it is clear that MSPEF dominates LPEF and CMA by 14.34 dB and 32.5 dB respectively. Secondly, it indicated that the CMA_MSPEF system overcomes the MSPEF by 2.25 dB.

Figures (12-17) indicate that the CMA_MSPEF system dominates the MSPEF by 5 dB, 5 dB and 2.25 dB for $SNR = 0, 5$ and 10 dB respectively for 16-QAM, and by 8 dB, 5 dB and 4 dB for 4-QAM under the same SNR's respectively.

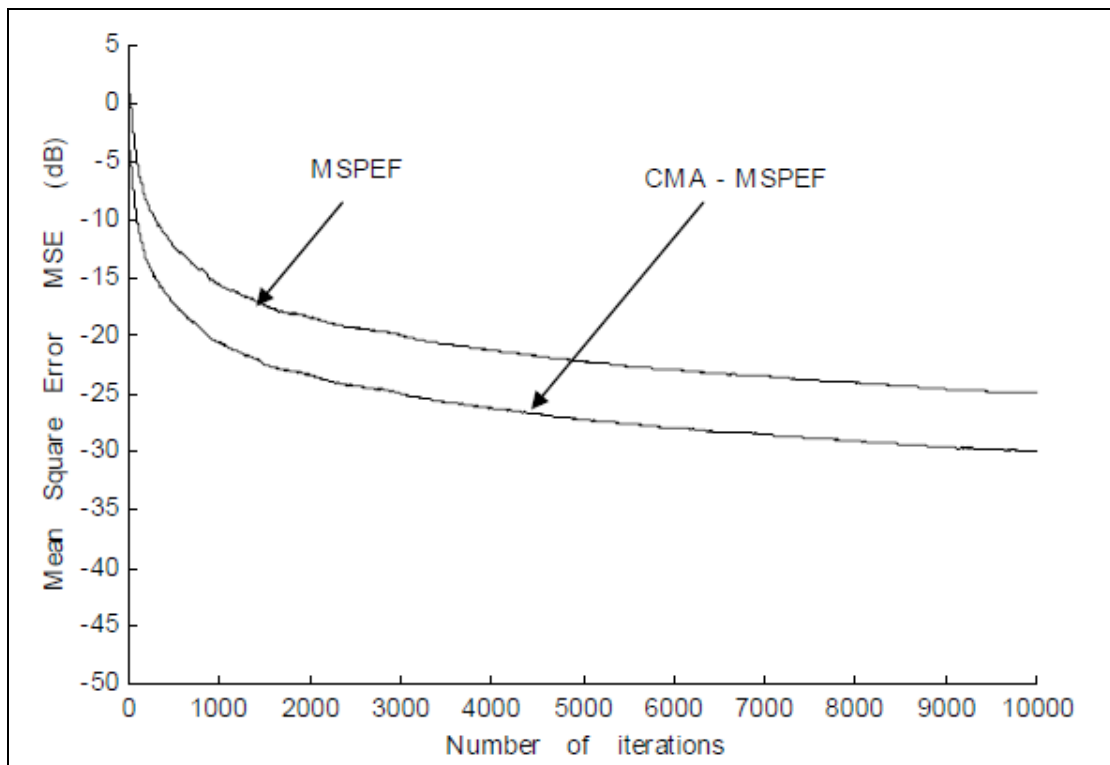


Fig.12. Coverage Curve for MSPEF, and CMA_MSPEF for 16 QAM, and Channel Two, with $SNR=0$ dB, and $D=8$.

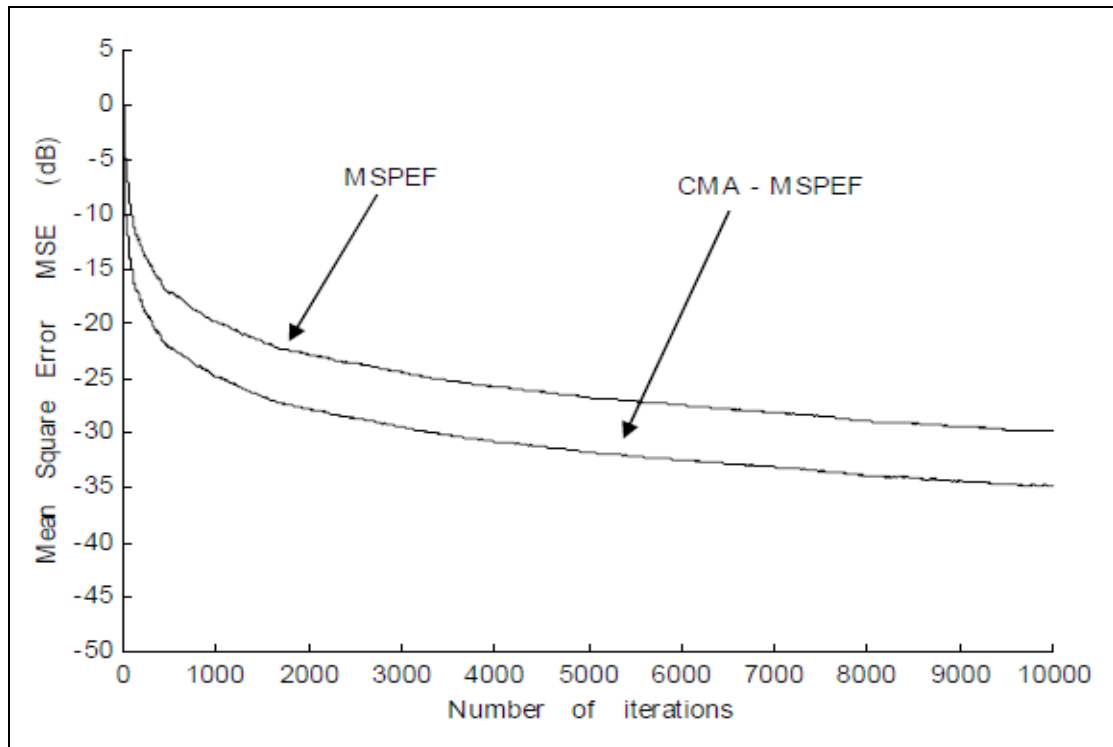


Fig.13. Coverage Curve for MSPEF, and CMA_MSPEF for 16 QAM, and Channel Two , with SNR=5 dB, and D=8.

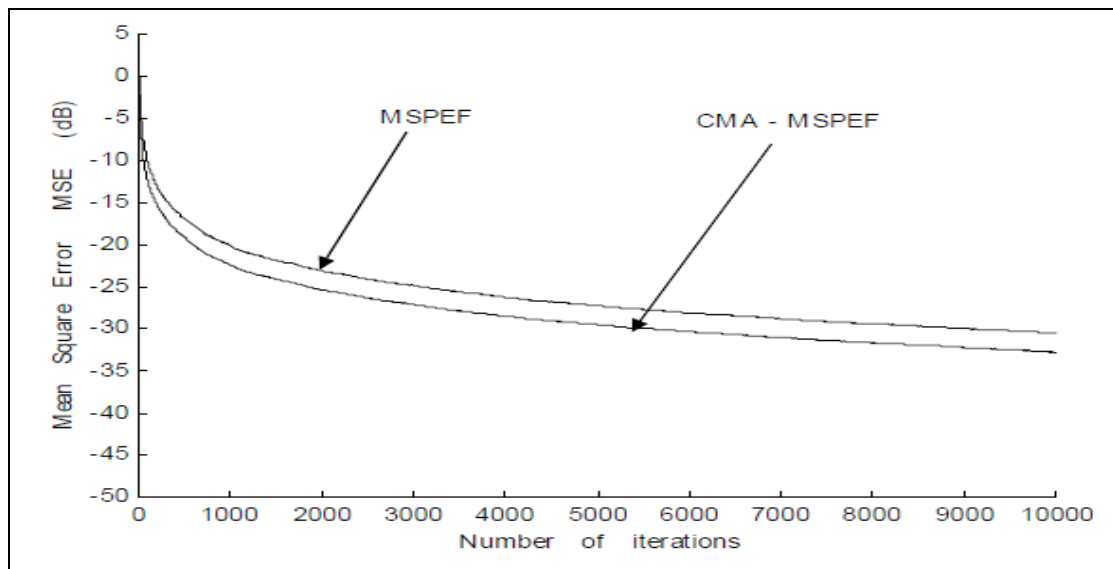


Fig.14. Coverage Curve for MSPEF, and CMA_MSPEF for 16 QAM, and Channel Two , with SNR=10 dB, and D=8.

Also for the same channel, $D = 8$, 16 QAM, and SNR=0, 5, 10 dB, we notice the figures (12-14) which show that also the proposed algorithm CMA_MSPEF dominates the algorithm MSPEF.

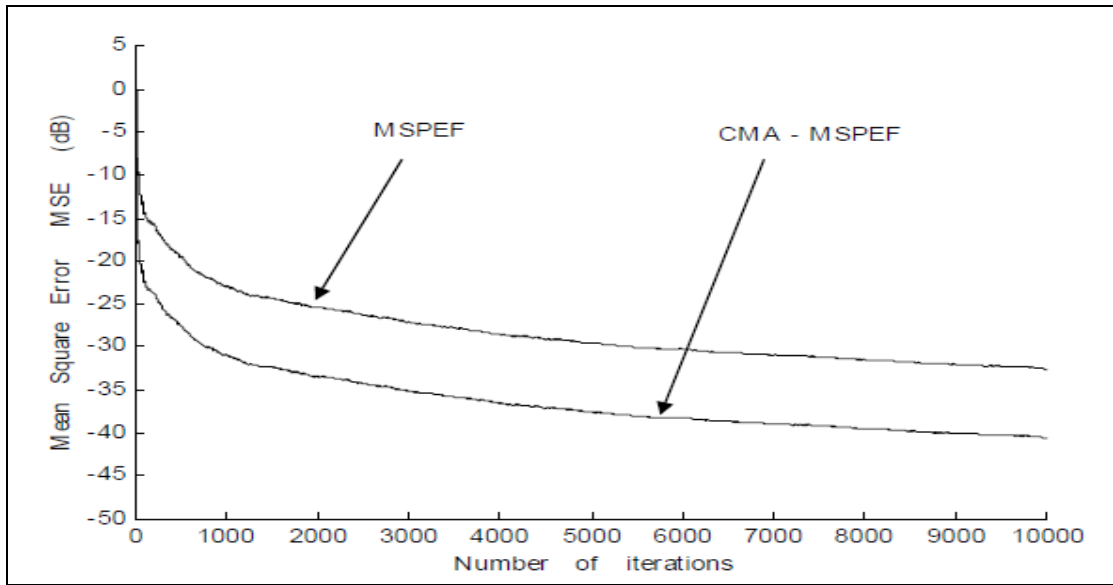


Fig.15. Coverage Curve for MSPEF, and CMA_MSPEF for 4 QAM, and Channel Two , with SNR=0 dB, and D=8.

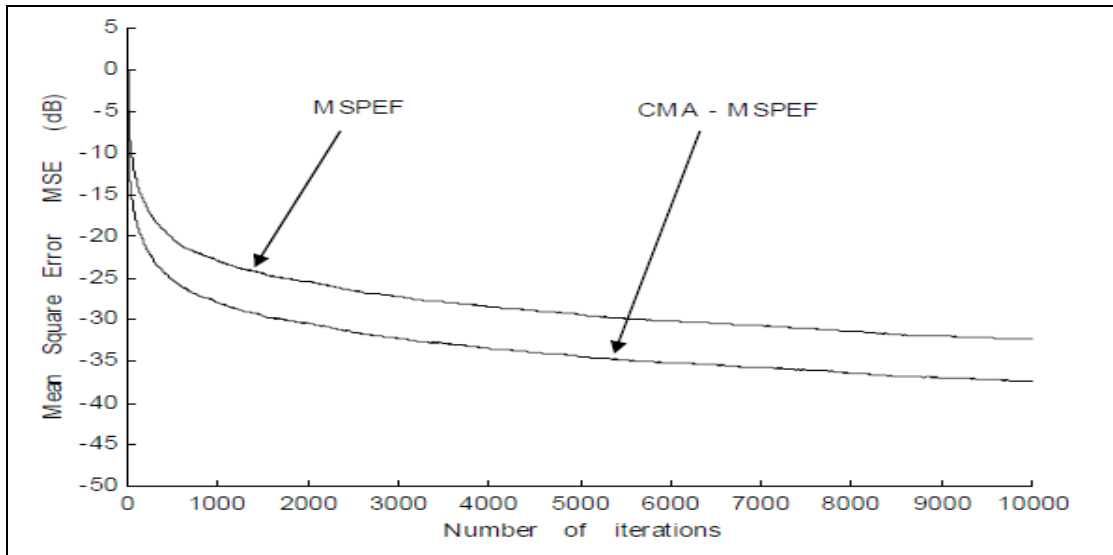


Fig.16. Coverage Curve for MSPEF, and CMA_MSPEF for 4 QAM, and Channel Two , with SNR=5 dB, and D=8.

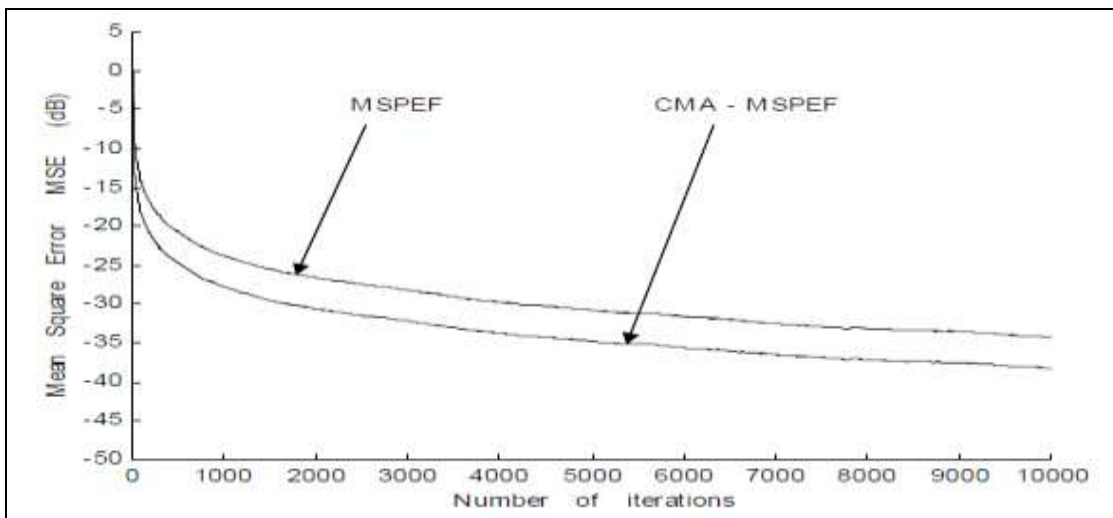


Fig.17. Coverage Curve for MSPEF, and CMA_MSPEF for 4 QAM, and Channel Two , with SNR=10 dB, and D=8.

Figures (15-17), show that the proposed algorithm CMA_MSPEF dominate the algorithm MSPEF for different SNR (0, 5, 10 dB), and D=8 for 4 QAM.

4. Convolution

In this paper, a new CMA_MSPEF blind equalizer which uses two techniques constant modulus algorithm cascaded with multi-step prediction error filter. This algorithm to overcome slow convergence of the conventional equalizers and to test the performance of this algorithm and to extract the optimum step value . It is clear that a cascade of CMA_MSPEF provides good performance. We can conclude that the CMA_MSPEF system is strongly recommended for its appreciable gain in performance when we use the optimum step calculated..

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