DC/DC Boost Converter Functionality in a Three-Phase IMC

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Abstract—An indirect matrix converter (IMC) connected with two input power sources is proposed: a gasoline generator as themain ac power supply and batteries as the secondary power source. The IMC is small in size because of having a dc-link part without an electrolytic capacitor. The dc-link part is utilized by connection with a boost-up chopper with batteries as a secondary input power source. Furthermore, the chopper connects to the neutral point of the motor and utilizes the leakage inductance of the motor as a reactor component. The proposed technique successfully further reduce the size of the converter by removing the boost reactor in the boost converter stage. The proposed converter is simulated and experimentally validated using a 750-W prototype and an induction motor driven with V/f control. The total harmonic distortion of the input and output currents are 4% and 3.7%, respectively, and the efficiency is 96%

Index terms—Synchronous Reference Frame, instantaneous current component theory, Modified SRF, Active Filter, Harmonics.

I. INTRODUCTION

Environmental responsibility has become a significant concern for communities so that the development of renewable power sources, such as wind turbines and lowcarbon emission hybrid electric vehicles (HEVs) is progressing rapidly. One of the most common applied converters in hybrid systems is the ac/dc/ac converter because it has the ability of connecting to two different power sources. The generator mainly supplies constant power to the load and a battery is used as an alternate power source to drive an electric motor and also to absorb the power fluctuation during periods of high peak energy demand. Fig. 1 shows a conventional ac/dc/ac power converter, which typically consists of a pulse width modulation (PWM) rectifier, a dc-link capacitor, and a PWM inverter, also known as a back to- back (BTB) system [1]-[3]. The PWM rectifier is often used to reduce the harmonic currents in a generator and control the dc-link voltage [2], [4]-[6]. In order to obtain high performance under an adjustable speed drive system, a constant dc-link voltage is required in a BTB system because the voltage fluctuation of the dc-link part will cause an output voltage error. A typi- cal method for reduction of the voltage fluctuation is to place a large electrolytic capacitor into the dc-link part as a filtering device between the rectifier and the inverter. However, a large electrolytic capacitor is bulky

Another approach is to reduce the capacity of the electrolytic

capacitor by the application of a high-speed dc-voltage controller to the rectifier control [7]. However, the control response is limited by the delay of the voltage detection and digital controller; therefore, the electrolytic capacitor is still required. In addition, the capacitance is not reduced, since the dc-link capacitor is dominated by the capacitor current. As a result, a large amount of space is required for the capacitor installation in a practical device. In addition, electrolytic capacitors are not suitable for high-temperature applications, such as in HEVs. Overall, these disadvantages of the electrolytic capacitor affect the reliability of the converter.



Fig. 1: Back-to-back converter.

For the secondary input power source, a boost converter that consists of a boost reactor and a switching leg [insulated gate

bipolar transistor (IGBT)] is connected with batteries to the dclink part of the BTB system. Boost converter will control the

battery current and the battery power will be used as a secondary power to drive the electric motor. In this paper, a new circuit topology is presented, which is composed of an indirect matrix converter (IMC) and a dc/dc boost converter that connects to the neutral point of a motor. An IMC has high efficiency and is easily configured in comparison to matrix converters [8]–[12]. In addition, this converter does not require a dc-link electrolytic capacitor to filter the dc-ripple voltage. It uses a direct conversion technique where the frequency of the dc-link voltage contains a ripple with

six times of the input frequency. However, the output voltage transfer ratio is limited by this direct conversion technique which is similar to the matrix converter, where output voltage = 0.866 of the input voltage [13].1)

Where x denotes voltages or currents.



Fig. 2: Proposed scheme

Nevertheless, an appropriate control over the inverter is also proposed so that it is possible to connect a dc chopper to the neutral point of the motor and to operate as a dc/dc converter [14]. This dc/dc converter with a battery is performed as a secondary power source of the IMC to drive the electric motor. The proposed circuit utilizes the neutral point of a motor in the boost converter because the leakage inductance of the motor can be used as a reactor. Generally, the leakage inductance is around

10% of the rating impedance in an induction motor. For the proposed dc converter, around 3% of the reactor is enough to use

as a boost reactor component. Please note that the synchronous

reactance in a permanent motor is higher than the leakage inductance of an induction motor. By removing the electrolytic capacitor and the boost-up reactor, the remaining part of the proposed circuit is constructed only of silicon components, namely, IGBTs and diodes. As a result, the proposed circuit is highly efficient and highly reliable. Simulation and experimental results clearly demonstrate that the circuit is capable of providing sinusoidal waveforms for the input and output, and high efficiency and a high power factor can be achieved.

II. PROPOSED CIRCUIT TOPOLOGY

Fig. 2 shows the proposed circuit configuration. The IMC

can be simply divided into primary and secondary stages. The

primary stage for the ac power source consists of 12 units of reverse-blocking IGBTs [15], also known as a current-source

rectifier, where bidirectional power flow is possible in this circuit

structure. A *LC* filter is required at the input of the primary stage

to smooth the input current. The secondary stage for the motor

consists of six IGBT units, which is similar to a standard voltage source inverter. The advantage of this converter over a BTB is

that the primary side does not contain switching loss because zero-current switching can be applied. The switching timing of

the primary side is during the zero-current period of the dc-link

when the secondary stage output zero voltage. Therefore, high

efficiency is achievable in this converter [11].

The other reason to use the IMC is that the IMC has a dclink mpart, which is different than the conventional matrix converter. The dc-link part is utilized by adding a boost converter to the IMC. The boost converter connects to the battery and the other

terminal of the battery is then connected to the neutral point of

the motor. A snubber circuit is also included in the dc-link part to absorb the voltage overshoot from reactive elements in the circuit [16]. It is used to prevent damage to the switching devices in the secondary side due to a sudden large voltage. It should be noted that the capacity of the snubber capacitor is smaller than the dc-link capacitor in a BTB system, because the ripple current of the dc-link part does not flow in the snubber capacitor. The chopper circuit is connected in the dc link and batteries are connected to the neutral point of the motor. The leakage inductance of the motor is used as a boost-up reactor in the proposed circuit. As a result, the proposed converter does not require bulky passive components.

Fig. 3(a) shows a control block diagram of the proposed

The primary side, the dc chopper, and the secondary side are

individually controlled by their own commands. A carrier comparison method is used as the PWM modulation, according

to the control strategy [17]. The relationship between the output

and input voltages is obtained by (1). The secondary side operates a four-phase voltage-source inverter by addition of thedc chopper as the fourth leg

$$\begin{bmatrix} v_u \\ v_v \\ v_w \\ v_{bat} \end{bmatrix} = \begin{bmatrix} s_{up} & s_{un} \\ s_{vp} & s_{vn} \\ s_{cp} & s_{cn} \end{bmatrix} \begin{bmatrix} s_{rp} & s_{sp} & s_{tp} \\ s_{rn} & s_{sn} & s_{tn} \end{bmatrix} \begin{bmatrix} v_r \\ v_s \\ v_t \end{bmatrix}$$
(1)

where s_{xy} represents the switching function of the switches. When s_{xy} is turned ON, $s_{xy} = 1$, and when s_{xy} is turned OFF, $s_{xy} = 0$.

A. Primary-Side Control

The primary-side controller is designed with a current-type

PWM rectifier command. It uses a pulse-pattern conversion to

convert the PWM pulses of the voltage source type into the PWM pulse of the current source type by a simple logic selector.

It uses a single-leg modulation where the switching period can be reduced from $2\pi/3$ to $\pi/3$, where the $2\pi/3$ is the switching

period of the conventional two-phase modulation [15]. That is, the leg with the maximum input phase voltage will always be

turned ON, and the other two legs will be always turned OFF,

as shown in Fig. 3(b). When the maximum input phase voltage

is changing, (for example, from +R-phase to -S-phase), the related max phase voltage leg and the mid phase voltage leg will

be switched at zero current until the relevant switch that contains

the mid phase voltage becomes the maximum input phase

voltage. From this direct conversion technique, a dc-link voltage

that contains a ripple with six times of the input frequency will

be formed [15].

B. Secondary-Side Control

A conventional controller method for a voltage-source-type

inverter is applied to the dc chopper and the inverter with a lean

controlled carrier modulation. The carrier modulation forms a



Fig. 3 (a) Control block diagram. (b) Primary-side-switching pattern

new carrier, where the peak position of the triangular carrier

is controlled by the duty ratio of the rectifier-side pulse. This rectifier pulse is used to control the switching timing of the primary stage and the zero-vector of the secondary stage. From

the control, zero-current switching is achieved in the primary

stage, where the dc-link current becomes zero at the peak of every carrier. This new carrier is then used in the secondary side

and the dc chopper side as a normal PWM comparison method,

also referred to as an inverter carrier.

The boost converter is not a stand-alone circuit in the proposed circuit. Operation is strongly dependent on the secondary side of the IMC. Zero-vector outputs on the secondary side are the key factor to link the boost converter to the IMC. The zero vector controls the amplitude of the output voltage. There are two functions of the zero-vector output to the secondary side. The first is to implement zerocurrent switching on the primary side so that the switching losses do not occur at the primary side. The second function involves operation of the boost converter, which will be described in a later chapter.Fig. 4 shows an example of the relationship between the normal carrier applied to the primary side and the new inverter carrier applied to the secondary side.

The inverter commands are given by the voltage controller as described in Chapter IV. It is noted that the dc chopper is controlled as the fourth leg of the inverter so that the dc chopper command is compared by the same carrier with the inverter voltage commands. There are two methods to generate an inverter carrier; Fig. 4(a) represents the symmetrical type, which has approximately double the switching frequency of the rectifier switching frequency, and Fig. 4(b) shows the asymmetrical type, which has the same switching frequency as the rectifier switching frequency [16]. min Fig. 4(a), the bottom peak position of the triangular carrier is controlled by the duty ratio of the rectifier pulse, as shown in



Fig. 4. Relationship between the zero vectors and boost converter operation.

(a) Symmetrical inverter carrier. (b) Asymmetrical inverter carrier

the upper part of the figure. The chopper commands, along with

the inverter output voltage commands, are compared with this

new inverter carrier to obtain the desired switching patterns. The

zero-vector periods are shown in the lower part of Fig. 4(a). The

switching pulses of the secondary side attain the zero vectors

for every carrier cycle. The primary side arms switch at every

zero-vector period.

In Fig. 4, zv_u and zv_l represent the zero-vector periods of the inverter, where $zv u = S_{up} = S_{vp} = S_{wp} = 1$ (upper arm zero vector) and $zv l = S_{up} = S_{vp} = S_{wp} = 0$ [lower arm zero vector ($S_{un} = S_{vn} = S_{wn} = 1$)]. The upper arm of the chopper (S_{cp}) switches ON at every zero-vector period of zv_u . On the

Other hand, the lower arm of the chopper (S_{cn}) will switch ON

at every zero-vector periods of zv_l. During these zero-vector

periods, the boost converter is operated in the ON-state, and the battery current through the leakage inductance of the motor

increases. During the nonzero-vector periods, also known as the OFF-state operation, the battery current is released into the

capacitor in the *LC* filter at the power source. The operation state in the figure is referred to the boost converter operation.

When the switching frequency of the rectifier is 10 kHz, the control method applied in Fig. 4(a) generates a new symmetrical

carrier that has a frequency of approximately 20 kHz. This

is approximately twice the primary-side switching frequency.

Alternatively, according to Fig. 4(b), an inverter carrier can be

formed based on the duty of the rectifier command, which is asymmetrical with a frequency of 10 kHz

By comparing the symmetrical and asymmetrical inverter carriers in Fig. 4, it should be noted that the zerocurrent n switching in the rectifier is not affected by the inverter carrier because

both carriers are formed following the rectifier duty. Since every

carrier time is longer in the asymmetrical inverter carrier, the

sequence of the zero-vector periods becomes slower; therefore,

the boost converter will achieve better efficiency, but the current

ripple in the battery will be increased. Further, the asymmetrical

method can achieve better total harmonic distortion (THD) values for the output because the deadtime effect is smaller due

to the lower switching frequency. The other disadvantage of the asymmetrical inverter carrier is the detection of the load current. Usually, the average value of the load current appears at the peak of the symmetrical inverter carrier so that it can be easily detected using the symmetrical inverter carrier. However, for the asymmetrical carrier, the average current point does not agree with the peak of the asymmetrical carrier; therefore, in order to detect the average current, a lowpass filter is required. Consequently, control performance will be decreased.

IV. UTILIZATION OF THE NEUTRAL POINT OF THE MOTOR

The voltage commands of the secondary stage are decided by the battery current command and the output voltage commands for the three-phase load. A three-phase inverter has eight output voltage space vectors, including two zero vectors. The importance of the zero vectors explains the behavior of the boost converter along with the neutral point of the motor. The boost converter will operate at every zero vector of the secondary side of the converter. On the other hand, the output voltage for the three-phase load is controlled by other voltage vectors, as shown in [14]. Fig. 5 illustrates the output current-flow diagram of the secondary side under the normal operation and Fig. 6 shows the zerophase-sequence equivalent circuit, where the battery is operating at discharge mode. In Fig. 5, the secondary side functions as a conventional three-phase inverter with a motor; it controls the motor speed and torque. Zero-phase sequence is happening at every zero-vector periods of the secondary side. The current at the neutral point of the motor is zero and a positive or negative battery current can be controlled, as shown in Fig. 6. Note that



Fig. 5. Secondary-side current flow diagram (normal operation)

the polarity of the battery voltage can be connected in facing the neutral point of the motor or in a reverse way [14]. C_{in} represents the capacitors from the *LC* filter; since two switches in the primary side will always be turned ON, the capacitors C_{in}

can be considered in the dc-link voltage. On the other hand, for

the zero-phase sequence, the motor line voltage can be considered as zero so that the motor can be considered as a leakage inductance. In addition, the secondary side of the converter can be considered as a single-leg topology. DC link voltage Single Leg Topology



The battery current first goes into the secondary side and flows out through the neutral line and charges or discharges the battery. The battery current can be controlled by the proportional–integral (PI) controller. The zero vectors are two particular vectors that generate zero line voltage to the motor. The neutral-point voltage vo of the motor, based on the neutral

point of the dc-link part, is obtained by the following equation:

$$Vo = E_{dc}/2 \text{ When all upper arms are ON}$$

v0 = -E_dc/2 When all lower arms are ON (3)

where E_{dc} is the dc-link voltage and v_0 is the voltage of the neutral point of the motor, based on the neutral point of the dc-link part. A high dc-link voltage is mandatory in order to control the zero vectors; therefore, the relationship between the dc-link voltage (E_{dc}), the inverter line voltage (v_{inv}), and the battery voltage (V_{bat}) will be discussed. The inverter output voltage, v_u , v_v , and v_w , with respect to the neutral point voltage of the

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Input voltage	200 V	DC source	100 V	$i_u = i_a + i_{bat}/s$ $i_v = i_b + i_{bat}/s$
Input frequency	50 Hz	Output voltage	173 V	iw = ic + ibave iw = ic + ibave where iu , iv , the positive-phase
Carrier frequency	10 kHz	Output frequency	35 Hz	
Inverter frequency	10 kHz	Leakage inductance	5 mH	

dc link, is expressed as

 $vu = aEdc/2sin \omega t + v0$

 $v_v = aEdc/2(\sin\omega t - 2\pi 3) + v_0$ $v_w = aEdc/2(\sin\omega t - 4\pi 3) + v_0$

(3)

where *a* is the modulation index of the motor phase voltage, 0 <

a < 1, vo is the neutral point voltage of the motor (during zero

phase sequence), and ω is the inverter output angular frequency.

The inverter line voltage is then given by (u-v phase)

 $v_{uv} = a\sqrt{3}/2 E_{dc} \sin(\omega t + \pi/6)$ (4) Equation (5) shows the relationship for an inverter to obtain the maximum output line voltage Vinv (rms) under the maximum

reference magnitude of a three-phase modulation

 $E_{dc} \ge 2\sqrt{2}/\sqrt{3}V_{inv}$. (5) The maximum line voltage between the inverter leg and chopper

leg can be obtained as (rms)

 $v_{ux} = \sqrt{2} \sqrt{3} V_{inv} + V_{bat}$ (6) Since v_{ux} must be smaller than E_{dc} , the inverter voltage and battery voltage are constrained by the following equation

$$Edc > \sqrt{2} / \sqrt{3} Vinv + Vbat$$
 (7)

As a result, the dc-link voltage of the proposed circuit must satisfy both requirements as shown by the following equation,

which can be referring to Fig. 6

$$E_{\rm dc} \ge \begin{cases} 2\frac{\sqrt{2}}{\sqrt{3}}V_{\rm inv}, & \text{When } \frac{\sqrt{2}V_{\rm inv}}{\sqrt{3}} \ge V_{\rm bat} \\ \frac{\sqrt{2}}{\sqrt{3}}V_{\rm inv} + V_{\rm bat}, & \text{When } \frac{\sqrt{2}V_{\rm inv}}{\sqrt{3}} < V_{\rm bat}. \end{cases}$$
(8)

Note that in (8), the V_{bat} can always be neutralized with half of the Edc under the two conditions. That is, Vbat must be always

smaller than half of the Edc, since the Edc is always known as

the 0.866 of the input phase voltage, as shown in the following

equation

 $\sqrt{2/2}$ Vin**0.866** > Vbat

Furthermore, a new expression of the secondary-side current

is given as follows, assuming that the leakage impedance is even

during the zero-phase-sequence equivalent circuit

(10)where i_u , i_v , and i_w are the inverter currents, i_a , i_b , and i_c are

positive-phase-inverter current, and *i*bat is the battery current

V. SIMULATION RESULTS

Table I shows the simulation parameters for both results. The

proposed circuit was simulated under two conditions of battery

discharge and charge. An automatic current regulator (ACR) ncontroller controls the battery current to a desired positive or negative value. An ideal battery current *i*bat is purposely adjusted

at a specific time of 38 ms to confirm the proposed circuit performance. The motor model, which consists of three sets of

voltage sources as back-electromotive forces and leakage inductances, is used in the simulation. The asymmetrical inverter

carrier was used in the simulation. Fig. 7 shows the battery discharge mode, with the battery current controlled from 0.5 to 2 A. The two waveforms show the input power supply voltages vr, vs, and vt, the input currents ir, is, and it, and the output line voltages (vuv(LPF), vvw(LPF), and vwu(LPF)) through a low-pass filter, which has a cutoff frequency of 1 kHz, to observe the low-frequency components, the output currents i_u , i_v , and i_w , and the battery current i_{bat} . The results show that the THD of both the input and output currents are less than 4%. It should be noted that at 20 ms. the input current magnitude decreases due to the increment of *i*bat, which indicates that the increase of the battery power leads to a decrease in generator power. On the other hand, Fig. 8 shows the ACR controlling the battery current from 0.5 to -2 A. The battery is charged from a generator under this condition. The results also showed that when in the charging mode, both the input and output currents have good sinusoidalwaveforms. At 20 ms, as the *i*bat decreases, the input current is forced to increase, because higher power is required to charge the battery. These two waveforms provide evidence of good power management between the generator and the battery.

i/p voltage,i/p current,o/p voltage,o/p current,battery current



(9)

Fig. 7. Simulation results (battery = discharge mode).

i/p voltage,i/p current,o/p voltage,o/p current,battery current



Fig. 8 Simulation results (battery = charge mode)

VII. CONCLUSION

A new control method is proposed by utilizing the neutral point of a motor and connection to an IMC for motor drive applications. Control over the inverter zero-vector periods allows an additional chopper leg to perform as a boost converter

with connection to the neutral point of a motor. Simulation results demonstrated good sinusoidal waveforms and confirmed the validity of the proposed method.

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