

# Optimal PID Controller Designing for Uncertain Bioreactor Using BFO Algorithm

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**Abstract** — Bioreactor plays major role in chemical, biochemical and pharmaceutical industries. The final product quality in a bioreactor depends mainly on the control system employed to supervise and regulate the process. In this article, modified Bacterial Foraging Optimization (BFO) algorithm supported PID controller design is attempted for the bioreactor operating at unstable steady state region. Weighted sum of multiple objective functions is considered as the cost function, which directs the BFO algorithm to find the optimal controller parameters. In this work, an uncertainty of  $\pm 10\%$  is assigned in the process model constraints such as process gain (K), time constant ( $\tau$ ) and delay time ( $\theta$ ). The BFO algorithm based search finds the minimal and maximal values of controller parameters such as  $K_p$ ,  $K_i$  and  $K_d$ . The competence of the proposed method has been confirmed through a simulation work. The results show that, the proposed method provides smooth performance in effective reference tracking with minimal error values.

**IndexTerms**— Bioreactor, modified BFO, uncertainty, multiple objective function, ISE.

Section 5 gives the simulated results followed by the conclusion of the present research work in section 6.

## I. INTRODUCTION

Biochemical reactor plays a vital role in chemical, biochemical and pharmaceutical industries to convert the raw material into marketable products such as beverages, antibiotics, vaccines and industrial solvents [1, 2]. The quality of final product in a bioreactor depends mainly on the control loop employed to control the microbial growth. Apart from this, incidental external and internal disturbances in a reactor may result in reactor failure. Hence, there is a strong economic motivation to develop an optimum control scheme to assist rapid start-up and stabilization of continuous bioreactors subject to redundant disturbances [4].

In the process control literature, a variety of methods have been discussed to employ a robust control scheme for the bioreactor operating at single or multiple steady states [3, 5]. PID controllers are still extensively employed in industrial process control systems because of their structural simplicity, reputation, robust behavior, and easy implementation [5,6]. The traditional PID tuning procedure existing for stable and unstable processes are model dependent and require numerical computations.

Recently, heuristic algorithm based PID tuning approach is extensively discussed in the literature because of its simplicity, high computational competence, easy execution and stable convergence [8-10, 19-21]. In this work, modified BFO supported PID controller design is proposed for a bioreactor operating at unstable operating region. The performance of the proposed tuning technique is evaluated with a simulation work.

The remaining part of the paper is ordered as follows: Description of bioreactor is provided in section 2, section 3 presents the summary of Bacterial Foraging Optimization algorithm. PID controller design is discussed in section 4.

## II. PROCESS DESCRIPTION

Bioreactor is a reactor system used to execute a number of biological reactions in a liquid medium to form intermediate and final products. Figure.1 depicts the diagram of a bioreactor [1, 2].

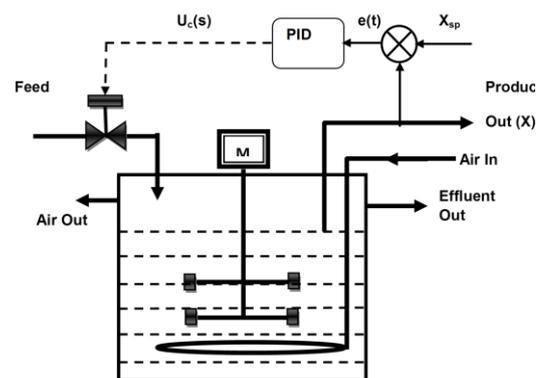


Figure 1 Illustration of a bioreactor

A number of studies are available in the literature for model based control of bioreactor [5,6,18]. In this work, a small scale bioreactor widely analysed by the researchers is considered and the corresponding mathematical equations are represented below [3,5];

$$\text{Cell balance} \quad : \quad \frac{dX}{dt} = (\mu - D)X \quad (1)$$

$$\text{Substrate balance} \quad : \quad \frac{dS}{dt} = D(S_f - S) - \frac{\mu X}{Y} \quad (2)$$

$$\text{Product balance : } \frac{dP}{dt} = -DP + (\alpha\mu + \beta)X \quad (3)$$

$$\text{Monod kinetics : } \mu = \frac{\mu_{\max} S}{K_m + S} \quad (4)$$

where, ' $\mu$ ' is specific growth rate, ' $X$ ' the biomass concentration, ' $S$ ' the substrate concentration and ' $\alpha$ ' and ' $\beta$ ' are yield parameters for the product. At steady state, the variables will be;  $X = X_s$ ,  $S = S_s$ , and  $P = P_s$ .

The unstable bioreactor model is a benchmark problem in the unstable system study. The unstable model is obtained with the following parameters;

$\mu_{\max} = 0.53 \text{ hr}^{-1}$ ,  $k_m = 0.12 \text{ g/lit}$ ,  $k_1 = 0.4545 \text{ lit/g}$ ,  $Y = 0.4$ . Steady state dilution rate is  $D_s = 0.3 \text{ h}^{-1}$  (the residence time is 3.33 h) and the feed substrate concentration is  $X_{fs} = 4.0 \text{ g/lit}$ . The nonlinear process has the three steady state operating points for a dilution rate of  $0.3 \text{ h}^{-1}$ . For the unstable operating region the biomass concentration value is  $X_{1s} = 0.9951$  and substrate concentration value is  $X_{2s} = 1.5122$ . The dilution rate is taken as the manipulated variable to control the cell mass concentration at the unstable steady state.

For the unstable operating region, the following linear model is obtained [3].

$$G_p(s) = \frac{-0.9951s - 0.2985}{s^2 + 0.1302s - 0.0509} e^{-\theta s} \quad (5)$$

$$= \frac{-5.8644}{5.89s - 1} e^{-\theta s} \quad (6)$$

Eqn. 5 represents the second order model and Eqn. 6 shows the first order model. The delay time ( $\theta$ ) for both the models is assigned as 0.1.

For uncertainty analysis, the first order model is considered and model perturbation of  $\pm 10\%$  is assigned for the process parameters like, process gain ( $K$ ), process time constant ( $\tau$ ) and delay time ( $\theta$ ) [23]. The general first order uncertain model is given in Eqn. 7.

$$G(s) = \frac{(K \pm \Delta K)}{(\tau \pm \Delta \tau)s - 1} e^{-(\theta \pm \Delta \theta)s} \quad (7)$$

### III. RELATED PREVIOUS WORK

In the literature, there exists a variety of methodology to analyze and control biochemical reactor. The detailed modelling procedure of the bioreactor is described in the books [1-3]. Zhao and Skogestad discussed various possible control configuration of the bioreactor system [4]. Pramod and Chidambaram discussed the identification and model based PID controller design for bioreactor operating at unstable steady state [6]. Rajinikanth and Latha proposed heuristic algorithms such as Particle Swarm Optimization (PSO) and BFO to tune the PID and modified structured PID controller for a class of unstable systems [8 -17]. A detailed modeling procedure for bioreactor is presented in the paper by Rajinikanth and Latha [18]. Roeva and Slavov discussed heuristic algorithm based PID controller design for an industrial type bioreactor [19 -21]. Slavov and Roeva discussed genetic algorithm based PID controller design to control glucose concentration in a bioreactor [22]. A detailed

description of PID and modified structured PID controller design for a class of unstable processes is discussed in the book by Padmasree and Chidambaram [5].

### IV. BACTERIAL FORAGING OPTIMIZATION ALGORITHM

Bacteria Foraging Optimization (BFO) algorithm is a population supported method, developed by inspiring the foraging manners of E.coli bacteria [7]. Due to its stable and superior convergence, it is widely considered to design PID controller for a class of time delayed unstable processes [10, 11, 15, 16]. In this paper, enhanced BFO algorithm discussed by Rajinikanth and Latha [13] is considered and the algorithm parameters are assigned as follows:

- Number of E.Coli bacteria =  $N = 20$
- Number of chemotactic steps ( $N_c$ ) =  $\frac{N}{2}$
- Swim length ( $N_s$ ) =  $\frac{N}{3}$
- Number of reproduction steps ( $N_{re}$ )  $\approx \frac{N}{3}$
- Number of dispersal events ( $N_{ed}$ )  $\approx \frac{N}{4}$
- Number of bacterial reproduction ( $N_r$ ) =  $\frac{N}{2}$
- Probability of the bacterial elimination/dispersal ( $P_{ed}$ ) =  $\left( \frac{N_{ed}}{N + N_r} \right)$
- Number of iterations during the search =  $N^2$
- Swarming parameters can be assigned as follows:

$$d_{atr} = W_{atr} = \frac{N_s}{N}; \quad \text{and} \quad h_{rep} = W_{rep} = \frac{N_c}{N}$$

### V. PID CONTROLLER DESIGN

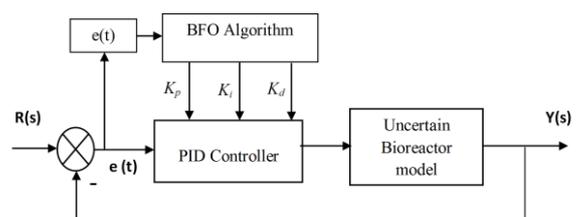


Figure 2 BFO algorithm based PID design

The parallel structure of PID controller is used to control the bioreactor. Mathematical representation of parallel structure of PID controller is presented in Eqn.8.

$$G_{PID}(s) = \left( K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1} \right) \quad (8)$$

where  $\tau_f$  if the filter time constant ( $\tau_f = \tau_d / N$  and  $N=10$ ).

The following performance criterion (Eqn.9) with three parameters, such as  $ISE$ ,  $M_p$  and  $t_s$  are considered in this work.

$$J(K_p, K_i, K_d) = (w_1 \cdot ISE) + (w_2 \cdot M_p) + (w_3 \cdot T_s) \quad (9)$$

where  $ISE = \int_0^T e^2(t) dt = \int_0^{100} [r(t) - y(t)]^2 dt$  (10)

$M_p = y(t) - r(t)$  (11)

$t_s$  = settling time ;  $T$  = total simulation time.

( $w_1, w_2$  and  $w_3$  are weighting parameters, to assign priority for cost functions and the value of 'w' varies from 0 to 1)

The performance measure  $J(K_p, K_i, K_d)$  monitors the BFO algorithm to get suitable values for PID controller. In this work, the following values are considered:

- Dimension of the search ( $D$ ) = 3
- The total number of E.Coli bacteria = 20
- The weighting function values are assigned as  $w_1 = 1, w_2 = 0.5$  and  $w_3 = 0.5$
- Search boundary is assigned as -100% and + 100% for  $K_p, K_i$  and  $K_d$ .

VI. RESULTS AND DISCUSSION

The performance of the proposed PID controller design is tested on the first order bioreactor model with parameter uncertainty. Ten trials are performed using the BFO algorithm and the best controller value among 10 trials is chosen as the optimal PID value.

The normal first order transfer function model of the unstable bioreactor is considered and the BFO algorithm based controller design is proposed with the method as shown in Figure 2. The multiple cost function based search is converged at 165<sup>th</sup> iteration with the following controller parameters;  $K_p = 0.5428, K_i = -0.1153$  and  $K_d = -0.3019$ . Final convergence of bacteria in the three dimensional search space is shown in Figure 3.

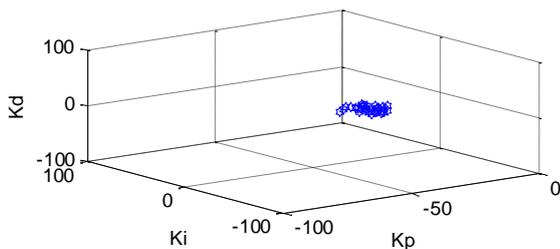


Figure 3 Convergence of E. coli bacteria

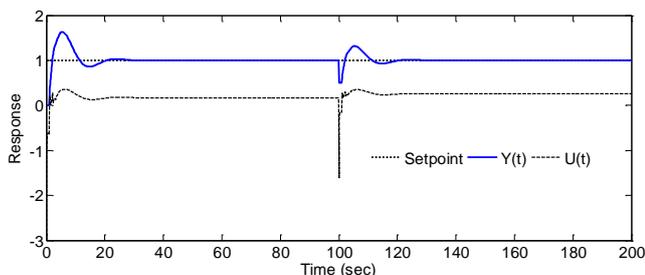


Figure 4 Servo and regulatory operations

Figure 4 depicts the servo and regulatory performances of the bioreactor with the above said PID controller parameters. A

setpoint of 0.9951 g / lit is applied and a load disturbance of 50% of setpoint is applied at 100 sec. From Figure 4, it is noted that, the PID controller provides a flat reference tracking and disturbance elimination performances with an overshoot of 0.572 g / lit and a settling time of 31.4 sec. The controller output ( $U(t)$ ) also smooth and it is free from the proportional and derivative kick effect.

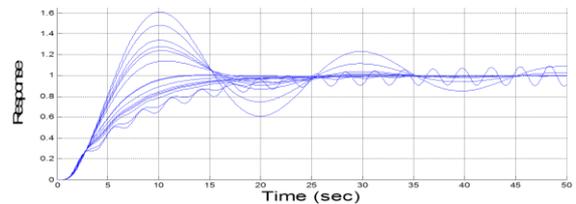


Figure 5 Reference tracking performance for the bioreactor model with ± 10% uncertainty

The performance of the above controller is then tested on the uncertain first order model of the bioreactor and the result is depicted in Figure 5. When the uncertainty is lesser than 10%, the controller provides a nearly stable response.

Finally, the robustness of the BFO based PID controller is examined using the nonlinear unstable bioreactor model developed with Eqn 1 – 4. A zero mean white noise signal with an amplitude of 0.1 is added in feedback path to test the reference tracking performance of the PID controller.

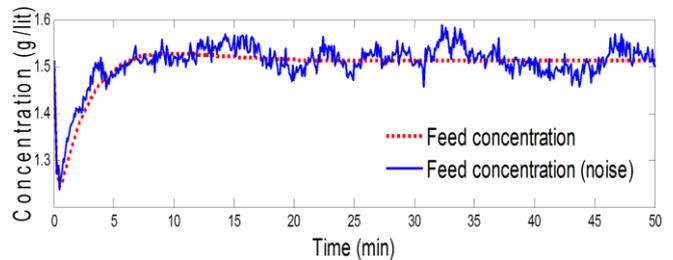


Figure 6 Variation of feed concentration

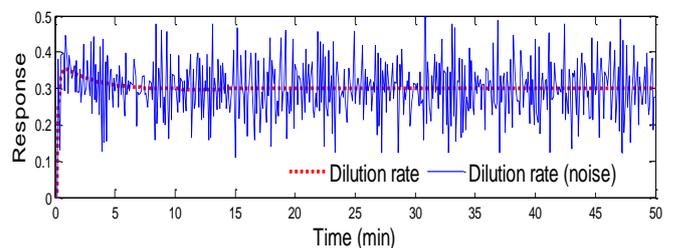


Figure 7 Variation of dilution rate

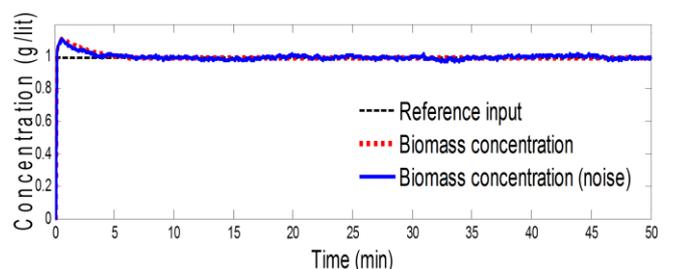


Figure 8 Variation of biomass concentration

Figure 6 and Figure 7 shows the variation of feed concentration and dilution rate respectively. Figure 8 depicts the change in biomass concentration. The rise time, overshoot and the settling time obtained for biomass concentration is excellent. From the above figures, it is noted that, the proposed PID controller provides a smooth response in the presence and absence of measurement noise signal and it works well on the nonlinear bioreactor model.

## VII. CONCLUSIONS

In this work, modified BFO algorithm based PID controller design is discussed for unstable bioreactor model with and without model uncertainty. The design of controller is formulated as an optimization problem using weighted sum of multiple objective function as the cost function. This method is a model free method, which provides the optimal controller parameters successfully. The result obtained from the simulation study shows that the discussed method works well in the linear and nonlinear model of the bioreactor and supports smooth set point tracking and disturbance rejection operations.

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